Section 2.3: Functions

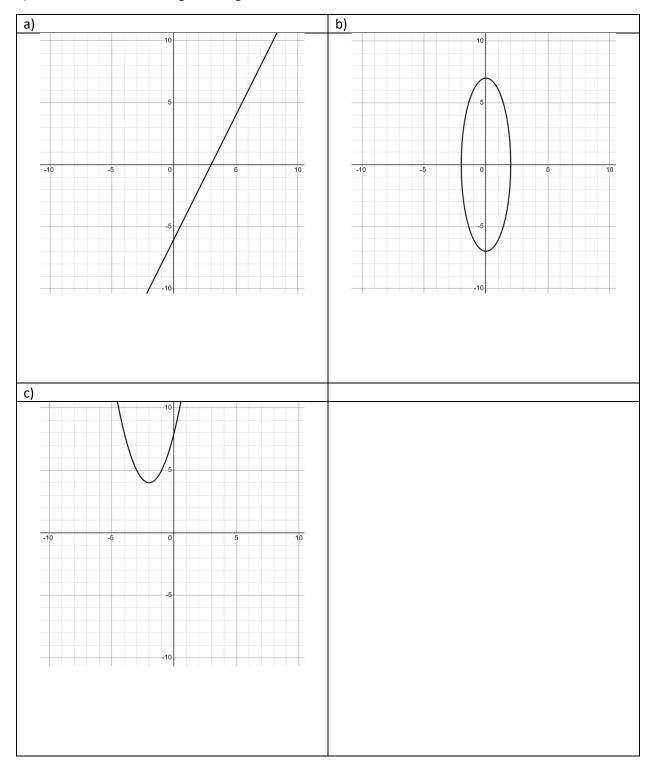
Video 1

A **relation** is a set of ordered pairs.

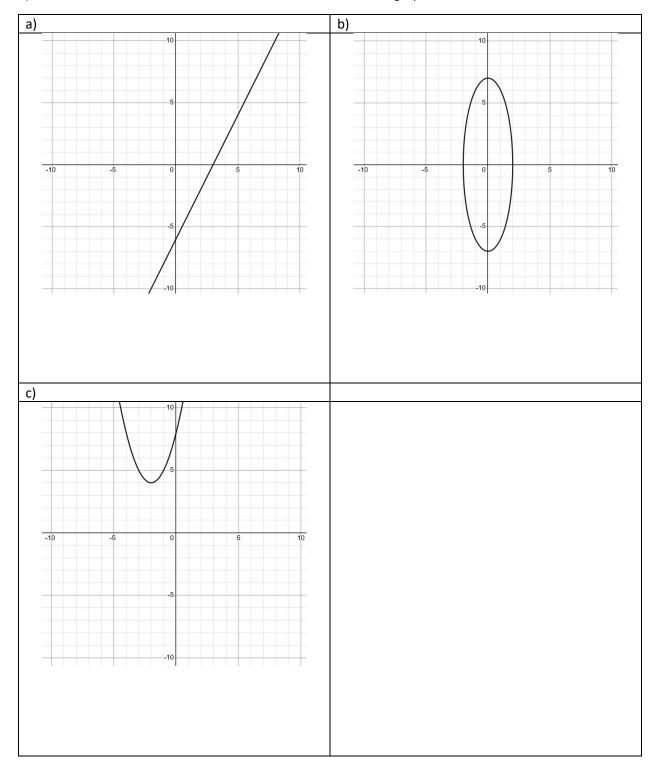
A **function** is a relation in which, for each distinct value of the first component of the ordered pairs, there is *exactly one* value of the second component.

1) List the domain and range of each relation. Does the relation define a function?

a) $\{(-2,9),(3,2),(8,9)\}$ b) $\{(4,2),(1,1),(0,0),(1,-1)\}$



2) Give the domain and range of the given relation.



3) Use the Vertical Line Test to determine if the relation that is graphed is a function.

4) Determine whether each relation defines *y* as a function of *x*, and give the domain and the range.

a)
$$y = 2x - 3$$
 b) $x = |y - 3|$

c)
$$y \ge 5x$$
 d) $y = \sqrt{x-4}$

e)
$$y = \frac{3}{x+6}$$

5) Let $f(x) = x^2 + 5x - 8$. Find the following.

a)
$$f(-3)$$
 b) $f(a)$

c) f(n+5)

6) Assume y is a function f of x. Rewrite each equation as a function of x, and find f(-6) and f(3).

a)
$$3x + 4y = 20$$

4) $y = x^2 - 6x - 10$

On an open interval I containing the points x_1 and x_2 ,

- A function f is increasing if $f(x_1) < f(x_2)$ whenever $x_1 < x_2$.
- A function f is decreasing if $f(x_1) > f(x_2)$ whenever $x_1 < x_2$.
- A function f is constant if $f(x_1) = f(x_2)$ whenever $x_1 < x_2$.

7) For the given function, determine the intervals for which the function is increasing, decreasing =, and constant.

